

# The CYBERNETIX and TERMA Case Studies in $\mu$ CRL

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- A general specification meta-language for describing the behavior of discrete event systems.
- Will include primitives for describing timed, probabilistic, stochastic and hybrid systems.
- Translations to the well-known formalisms like UPPAAL, SPIN, CADP, MÖBIUS,  $\mu$ CRL, etc., should enable efficient analysis.

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- Deals with a card personalization conveyor.
- The goal is in finding an optimal schedule.
- An idea is in trying model checking techniques for timed systems.

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- An UPPAAL model by Tomas Krilavičius (UT, The Netherlands).
- A similar model in SPIN by Theo Ruys (UT, The Netherlands).
- Two  $\mu$ CRL models, similar to the models of Biniam and Tomas, respectively.

What does similar mean?

Why are these models related to MoDeST?

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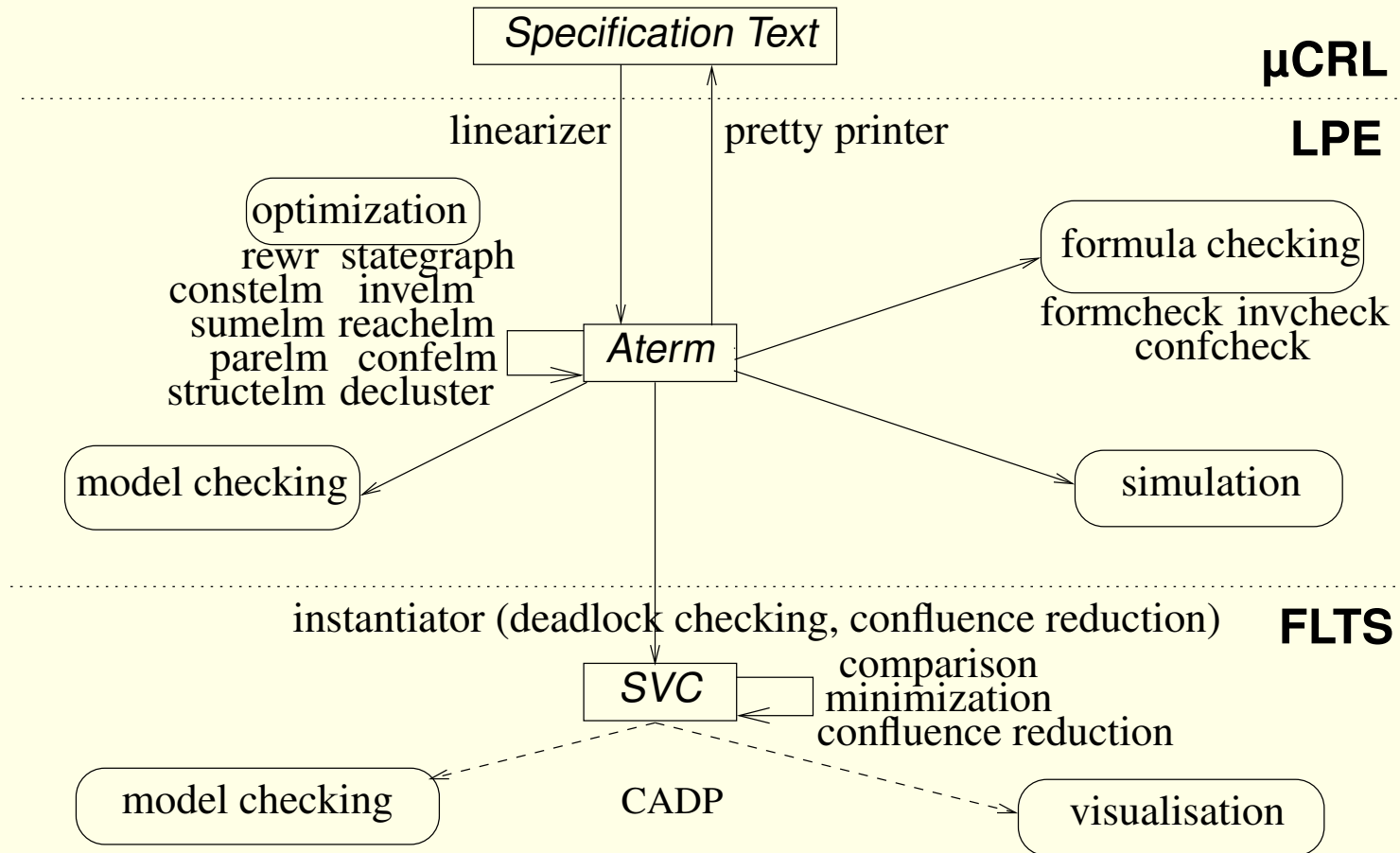
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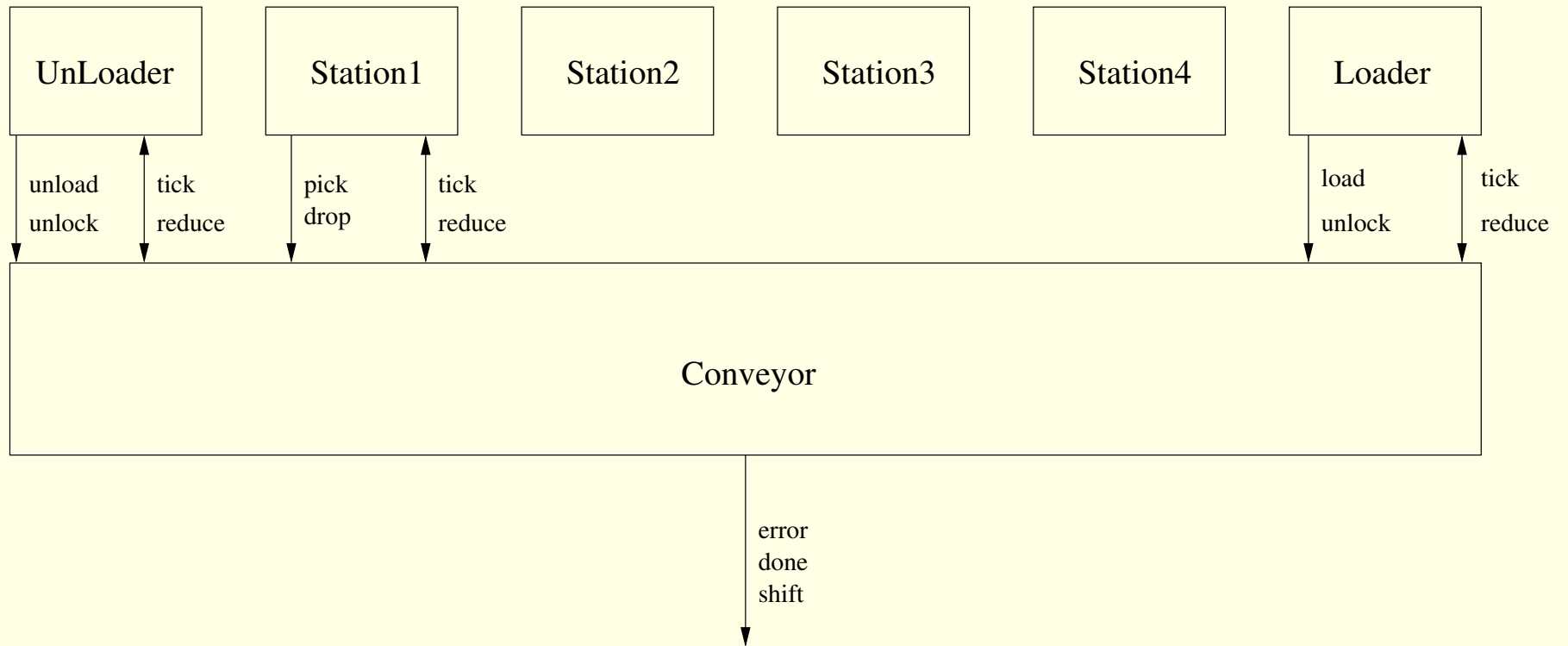
Extensions to process algebra:

- action parameterized by data ( $a(d) \mid b(e) \approx c(d) \triangleleft d = e \triangleright \delta$ ),
- $\sum_{d:D} p$  and  $x \triangleleft c \triangleright y$
- systems of parameterized recursion equations.

# Overview of the $\mu$ CRL Toolset



## The CYBERNETIX CS in $\mu$ CRL



What are the differences between the models of Beniam and Tomas?

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- Technically, this is achieved by using action renaming and synchronous communication.



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- For the model similar to Tomas' we could analyze all the systems presented by Tomas and Theo on the previous AMETIST meetings in Twente and Dortmund, respectively.
- For the case of 4 stations and 8 cards we could find an optimal schedule which is 1 tick better than the one found by Theo (46 instead of 47 ticks).

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- In the model we do not store the global time.
- After each loaded card we decrease each card number in the system (on the conveyor, in the stations, the next card to be loaded) by 1. This is done by synchronizing all processes on **reduce** action.



## Finding an Optimal Loop (cont.)

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- The future plans are finding these optimal loops and trying to analyze the model with 5 or more stations in this way.

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- Fixing a particular concrete formulation of the case study allows the academic partners to compare the tools and techniques by trying to find concrete optimal schedules.

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